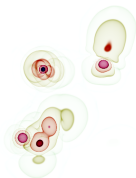


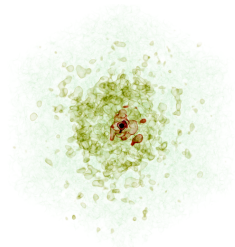
Small-scale features in fuzzy dark matter cosmology



Philip Mocz

Princeton

Oct 2, 2018



A. Fialkov (Cambridge), L. Lancaster (Princeton), PH. Chavanis (Toulouse), M. Vogelsberger (MIT),
M. Amin (Rice), J. Ostriker (Columbia), B. Church (Columbia)



XSEDE

Einstein Oct 2 2018

Outline

- ▶ Intro to Fuzzy Dark Matter (FDM)
 - ▶ motivation
 - ▶ observational constraints
- ▶ Simulations of virialized halos (Mocz et al., 2017)
 - ▶ halo properties
 - ▶ quantum turbulence in halos
- ▶ Numerical methods
 - ▶ spectral (Mocz et al., 2017)
 - ▶ SPH (Mocz & Succi, 2015)
- ▶ Schrödinger/Vlasov–Poisson correspondence (Mocz et al., 2018)
 - ▶ Does a 3D wave function encode 6D collisionless dynamics for large m ?
- ▶ Full-physics cosmological simulations (PM+ in prep)
- ▶ Dynamical Heating / Friction (Church, PM, Ostriker 2018; PM+ in prep)
- ▶ Direct radial collapse and soliton cores (PM+ in prep)

What is fuzzy dark matter?

What if dark matter is ... *very light*?

- ▶ Assume DM is a cold, ultralight scalar field (Peebles, 2000; Hu, Barkana & Gruzinov, 2000; Schive et al., 2014; Schwabe, Niemeyer & Engels, 2016)
- ▶ $T = 0$ in early universe, forms a BEC \Rightarrow **macroscopic quantum properties**
- ▶ Uncertainty principal suppresses gravitational collapse below de Broglie wavelength
- ▶ Require $m \sim 10^{-22}$ eV to get $\lambda_{\text{DB}} \sim 1\text{kpc}$ for $10^8 M_{\odot}$, $z = 5$ halo virial velocity (Chavanis, 2011)
- ▶ **Schrödinger-Pitaevski-Poisson** equation evolution

$$i\hbar \frac{\partial \psi}{\partial t} = -\frac{\hbar^2}{2m} \nabla^2 \psi + mV\psi, \quad \nabla^2 V = 4\pi G(\rho - \bar{\rho}), \quad \rho = |\psi|^2 \quad (1)$$

Properties: Soliton core solutions

Stable soliton core solutions (Schive et al., 2014)

$$\rho_{\text{soliton}}(r) \simeq \rho_0 \left[1 + 0.091 \times \left(\frac{r}{r_c} \right)^2 \right]^{-8} \quad (2)$$

where

$$\rho_0 \simeq 3.1 \times 10^{15} \left(\frac{2.5 \times 10^{-22} \text{ eV}}{m} \right)^2 \left(\frac{\text{kpc}}{r_c} \right)^4 \frac{M_\odot}{\text{Mpc}^3} \quad (3)$$

- ▶ core + r^{-16} outer profile
- ▶ more massive = more compact

Motivation for FDM

▶ Astrophysics

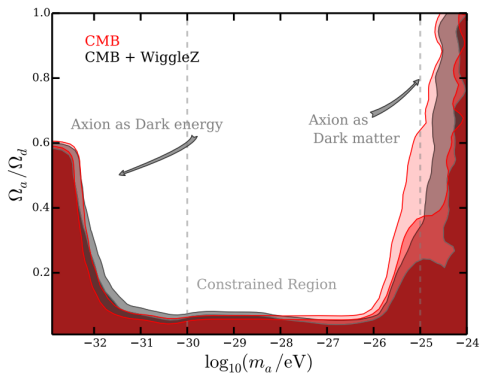
▶ Λ CDM small scale shortcomings

- ▶ deficit of dwarf galaxies (missing satellites problem Klypin et al. 1999; Moore et al. 1999)
- ▶ problem with the abundance of isolated dwarfs (Zavala et al., 2009; Papastergis et al., 2011; Klypin et al., 2015)
- ▶ too-big-to-fail problem (Boylan-Kolchin, Bullock & Kaplinghat, 2011, 2012)
- ▶ cusp-core problem (Moore, 1994; Flores & Primack, 1994; Gentile et al., 2004; Donato et al., 2009; de Blok, 2010)

▶ Theoretical Physics

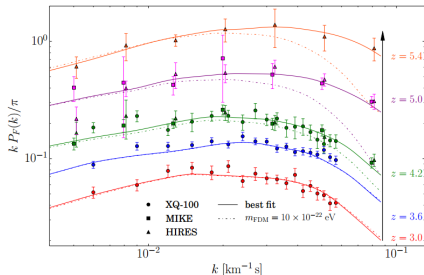
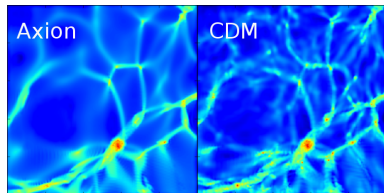
- ▶ Ultralight axions solve the strong CP problem in QCD (Peccei-Quinn theory; $m \sim 10^{-5} - 10^{-3}$ eV)
- ▶ String-theory compactifications provide class of ultralight axions ($m \sim 10^{-22}$ eV) (Arvanitaki et al., 2010)

Axion mass constraints from CMB



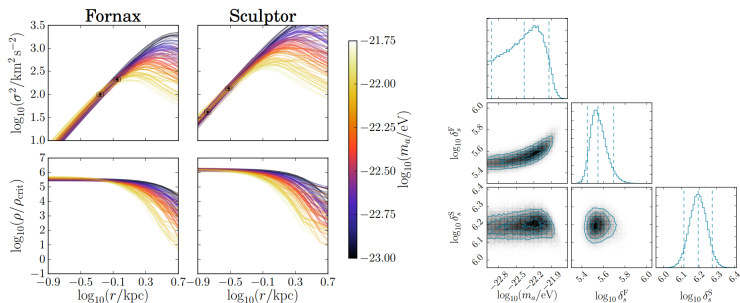
- ▶ Axion can't be too light, else λ_{dB} is inconsistent with CMB fluctuations: $m \geq 10^{-24}$ eV

Axion mass constraints from Ly- α forest



- ▶ Current studies consider the cut-off in the linear matter power spectrum and make analogies to WDM, using collisionless N -body hydro simulations. Quantum/wave effects are ignored. Armengaud et al. (2017); Iršič et al. (2017)
- ▶ suggest $m \gtrsim 10^{-21}$ eV, but remains to be verified by fully self-consistent simulations

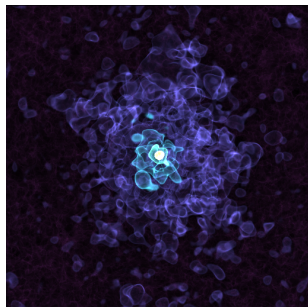
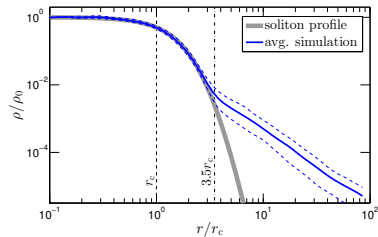
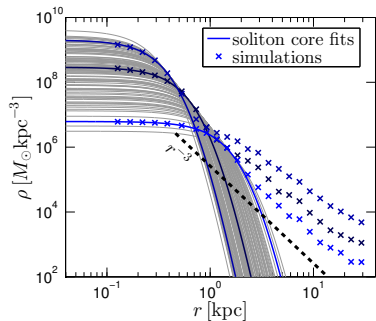
Axion mass constraints from Dwarf Spheroidals



- ▶ Model DM-dominated dwarf spheroidal galaxies (Fornax, Sculptor) with pure soliton core potential e.g., Marsh & Pop (2015); Gonzalez-Morales et al. (2016)
- ▶ suggest $m \lesssim 10^{-22}$ eV

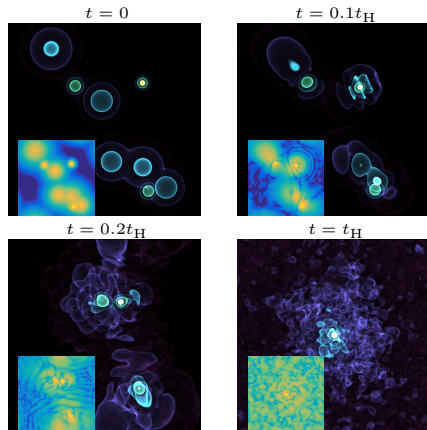
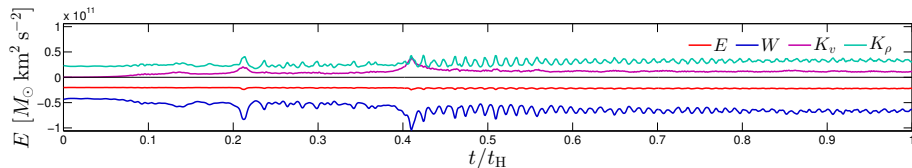
- ▶ Galaxy formation with BECDM – I. Turbulence and relaxation of idealized haloes (Mocz et al., 2017)
 - ▶ simulate virialized DM halos
 - ▶ virialized profiles
 - ▶ self-similarity? soliton core-halo mass relation
 - ▶ quantum turbulence

FDM profiles



- ▶ Soliton core ($r^0 \rightarrow r^{-16}$)
- ▶ NFW-like outer profile (r^{-3}) or flatter (r^{-2} isothermal)
- ▶ c.f. NFW ($r^{-1} \rightarrow r^{-3}$)

FDM energies



▶ Energies:

▶ $W = \int \frac{1}{2} \rho V d^3x$

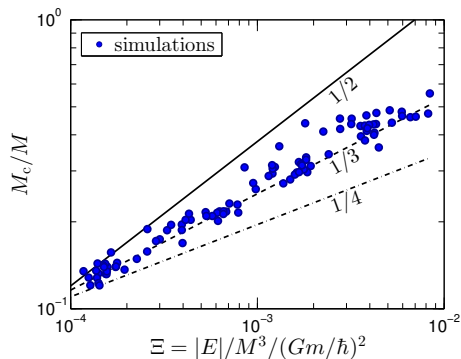
▶ $K_v = \int \frac{1}{2} \rho v^2 d^3x$

▶ $K_{\rho} = \int \frac{\hbar}{2m^2} (\nabla \sqrt{\rho})^2 d^3x$

▶ Approx. virial equilibrium:

$$|W| = 2(K_v + K_{\rho})$$

FDM soliton cores



► scaling symmetry:

- $t \rightarrow \lambda^2 \hat{t}$
- $x \rightarrow \lambda^{-1} \hat{x}$
- $\psi \rightarrow \lambda^2 \hat{\psi}$
- $M \rightarrow \lambda M$
- $E \rightarrow \lambda^3 E$

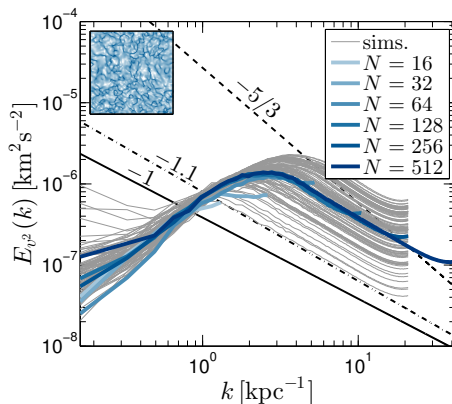
► find:

$$M_c/M \propto (|E|/M^3)^{1/3}$$

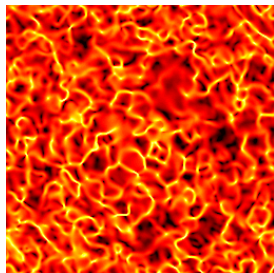
fundamental relation

- means core & halo binding energy in equipartition
- previously reported relation $M_c \propto (|E|/M)^{1/2}$ (Schive et al., 2014) actually is just scaling symmetry

FDM quantum turbulence



- ▶ similar to ‘thermal’ turbulence seen in condensed matter BEC systems: thermal bump, k^{-1}
- ▶ Kolmogorov $k^{-5/3}$ may be possible if system driven at largest scales



Numerical methods

- ▶ spectral (Mocz et al., 2017)
- ▶ SPH (Mocz & Succi, 2015)

Spectral (Mocz et al., 2017)

2nd-order in time leap-frog scheme. ‘Kick-drift-kick’

- ▶ Calculate potential:

$$V = \text{ifft} \left[-\text{fft} [4\pi G(\rho - \bar{\rho})] / k^2 \right] \quad (4)$$

- ▶ Potential half-step ‘kick’:

$$\psi \leftarrow \exp [-i(\Delta t/2)(m/\hbar)V] \psi \quad (5)$$

- ▶ Full ‘drift’ (kinetic) step in Fourier-space:

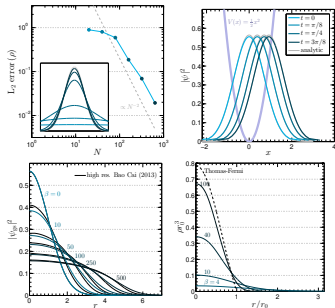
$$\hat{\psi} = \text{fft} [\psi] \quad (6)$$

$$\hat{\psi} \leftarrow \exp \left[-i\Delta t(\hbar/m)k^2/2 \right] \hat{\psi} \quad (7)$$

$$\psi \leftarrow \text{ifft} [\hat{\psi}] \quad (8)$$

- ▶ Another ‘kick’

SPH (Mocz & Succi, 2015)



- Madelung fluid form, use SPH estimate of quantum pressure tensor

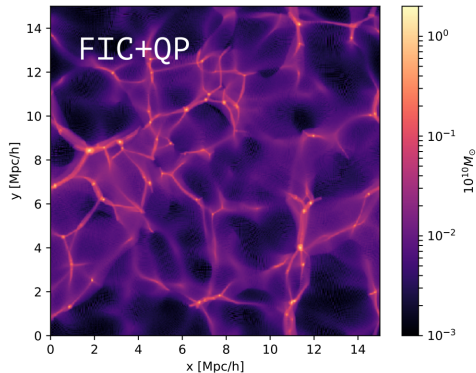
$$\partial_x \rho_i = \sum_j m_j \partial_x W_{ij}.$$

$$\partial_{xy} \rho_i = \sum_j \frac{m_j}{\rho_j} (\rho_j - \rho_i) \partial_{xy} W_{ij},$$

$$P_{i,xy} = \sum_j \frac{m_j}{\rho_j} \frac{1}{4} \left[\frac{(\partial_x \rho_j)(\partial_y \rho_j)}{\rho_j} - \partial_{xy} \rho_j \right] W_{ij}$$

- Lagrangian, adaptive
- can add viscosity \Rightarrow find ground states!

SPH: AX-Gadget (Nori & Baldi 2018)

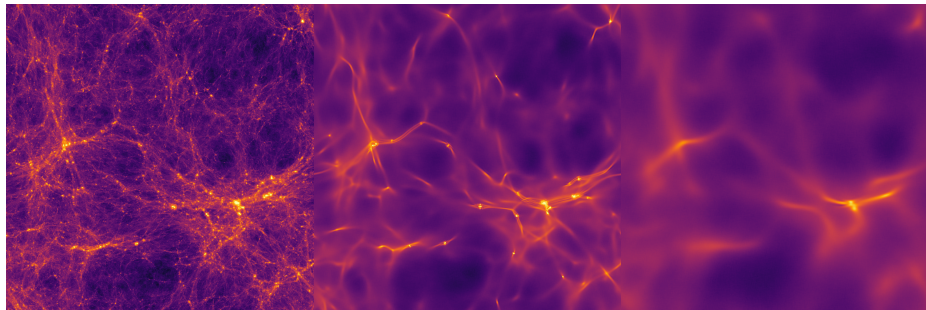


- ▶ captures large-scale quantum pressure
- ▶ based on SPH idea (Mocz & Succi, 2015)

Cosmological simulations

Cosmological simulations

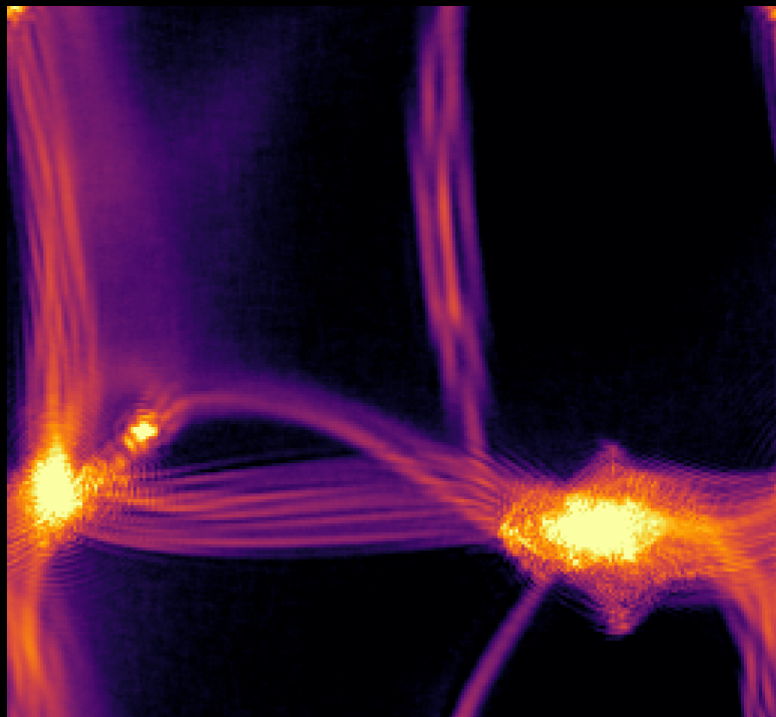
- ▶ Added to AREPO, coupled with baryon model with feedback
- ▶ self-consistent quantum wave effects, baryon coupling

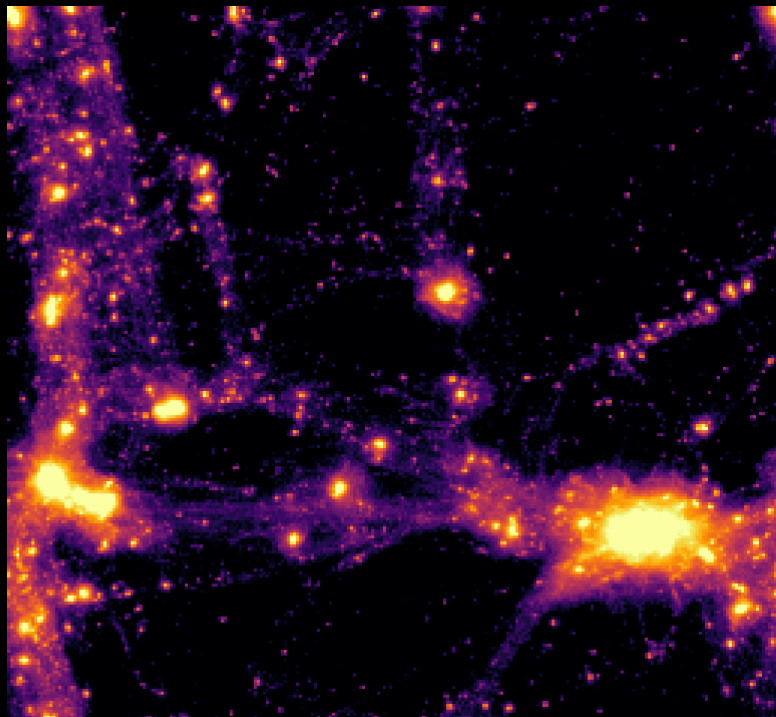


Λ CDM

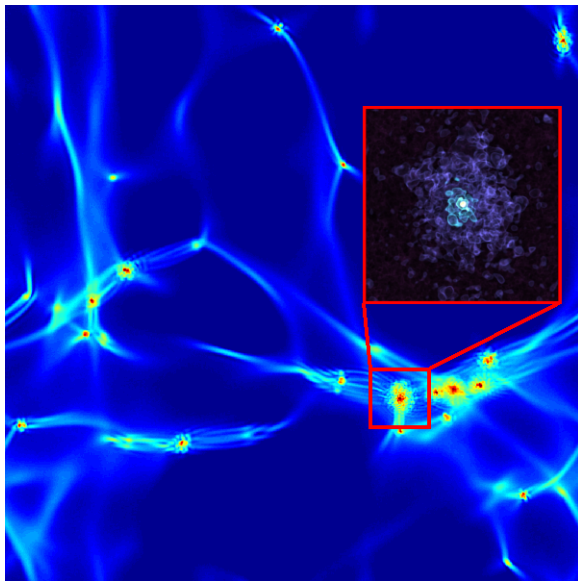
$2.5e-21$ eV

$2.5e-22$ eV





Cosmological sims: idealized sims in context



- ▶ Turbulent relaxed cores found in cosmological simulations

Schrödinger/Vlasov–Poisson correspondence

Limiting behaviour for large boson mass (e.g., QCD axion)
(Mocz et al., 2018)

- ▶ do the 3D Schrödinger equations encode collisionless dynamics (6D)?

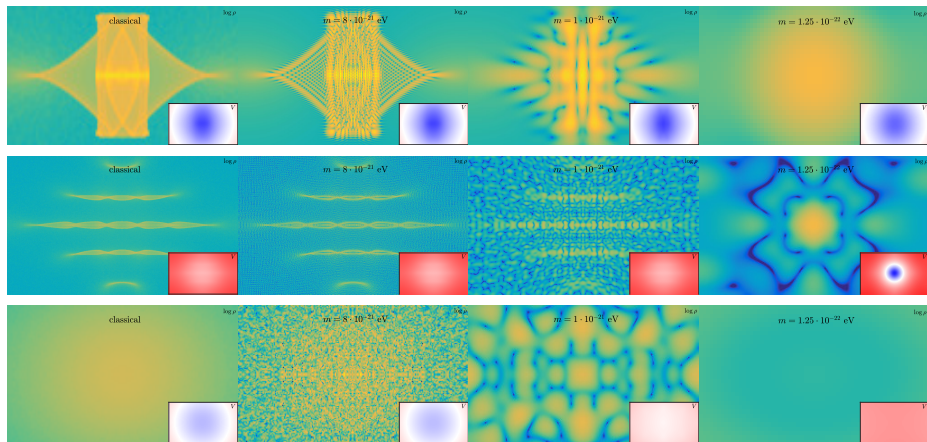
$$i\hbar \frac{\partial \psi}{\partial t} = -\frac{\hbar^2}{2m} \nabla^2 \psi + mV\psi \quad (9)$$

$$\iff (?)$$

$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \frac{\partial f}{\partial \mathbf{x}} - \nabla V \cdot \frac{\partial f}{\partial \mathbf{v}} = 0 \quad (10)$$

Schrödinger/Vlasov–Poisson correspondence

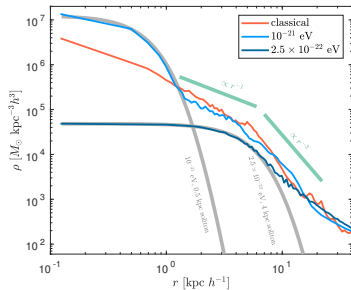
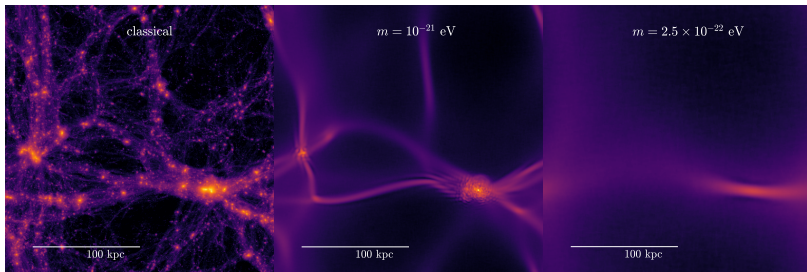
(Mocz et al., 2018)



$$\psi(\mathbf{x}) \propto \sum_{\mathbf{v}} \sqrt{f(\mathbf{x}, \mathbf{v})} e^{im\mathbf{x} \cdot \mathbf{v}/\hbar + 2\pi i \phi_{\text{rand}, \mathbf{v}}} d^3v$$

$V \rightarrow V_{\text{classical}} \text{ as } m^{-2}$

Schrödinger/Vlasov–Poisson correspondence

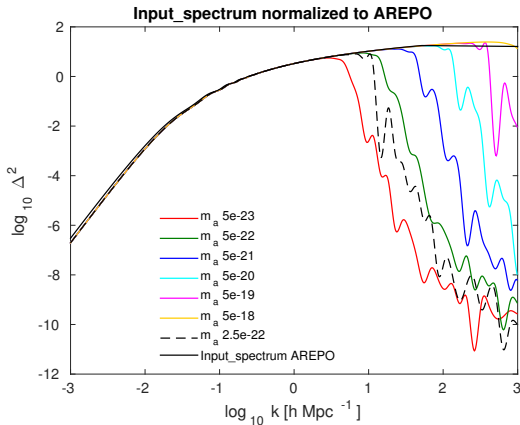


Full-physics cosmological simulations

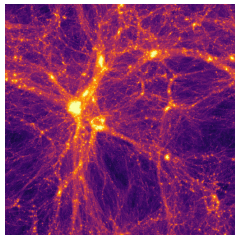
BECDM + hydrodynamical simulations with galaxy formation physics

(PM+in prep.)

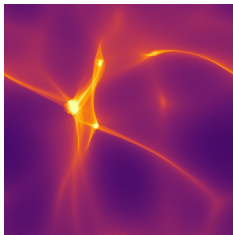
- ▶ $m = 2.5 \cdot 10^{-22}$ eV axion
- ▶ axionCAMB initial conditions



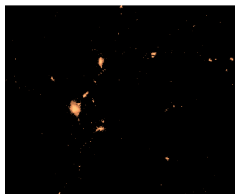
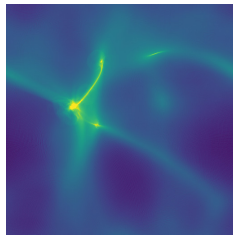
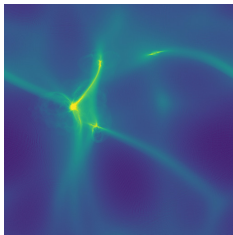
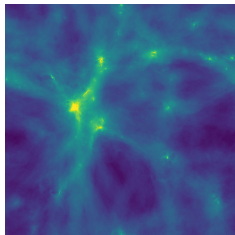
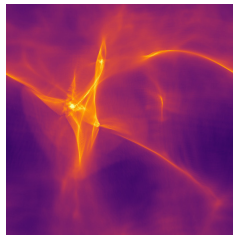
$z = 5$, Λ CDM



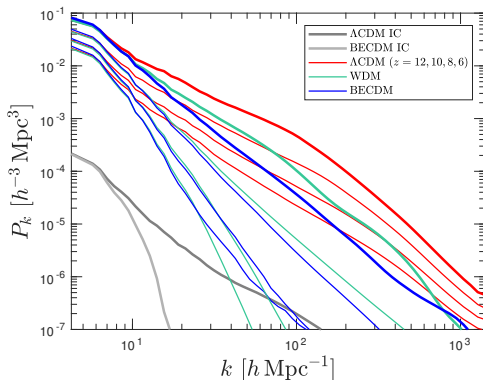
WDM



BECDM

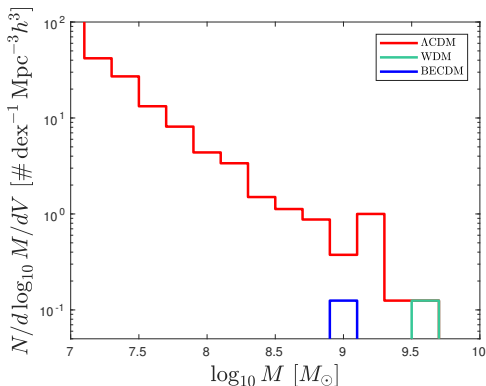


DM power spectrum



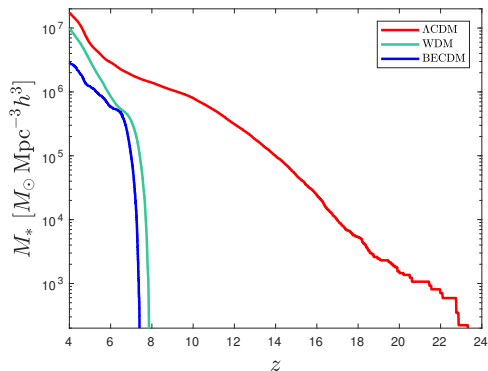
- ▶ quantum pressure tensor adds extra suppression of small-scale power
- ▶ agreement with CDM above 1 Mpc

“Halo mass function” ($z = 6$)



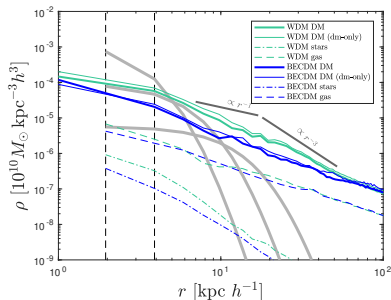
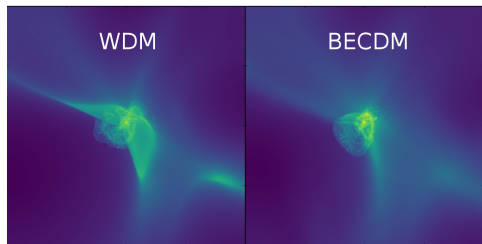
- ▶ $m = 2.5 \cdot 10^{-22}$ eV axion erased all structure below $10^9 M_{\odot}$

Cosmic Star formation history



- ▶ star formation hugely delayed

Radial profiles



- ▶ quantum pressure tensor smooths out caustic-tracing baryon structure
- ▶ soliton cores form late ($z < 6$)
- ▶ can see r^{-2} isothermal profiles for such low axion mass

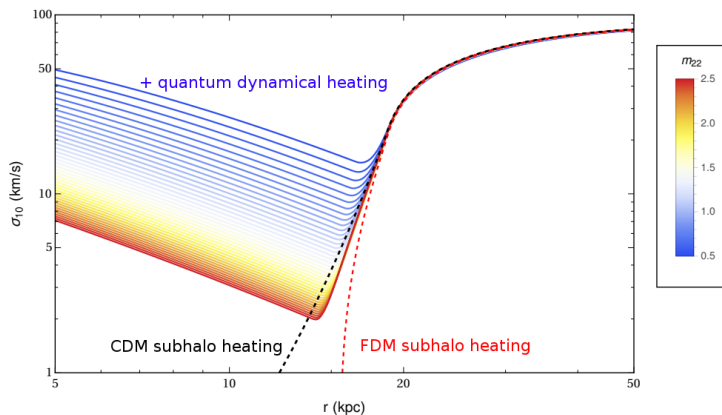
Qualitative effects to be quantified ...

- ▶ formation of first stars & galaxies delayed
- ▶ filaments are formation sites for stars
- ▶ interference granules heat baryons
- ▶ suppression in power spectrum at small scales
- ▶ soliton cores (halo relationship, baryonic modifications)
- ▶ stellar populations, galaxy sizes, JWST image predictions

Dynamical Heating (Church, PM, Ostriker subm)

- ▶ quantum interference patterns heat / thicken discs
- ▶ \Rightarrow stochastic solenoidal force-field, random-walk

$$\frac{d\sigma_D^2}{dt} = \int_{b_{\min}}^{b_{\min}} (2\pi b) db n v_p \left(\frac{M_I G}{b v_p} \right)^2$$

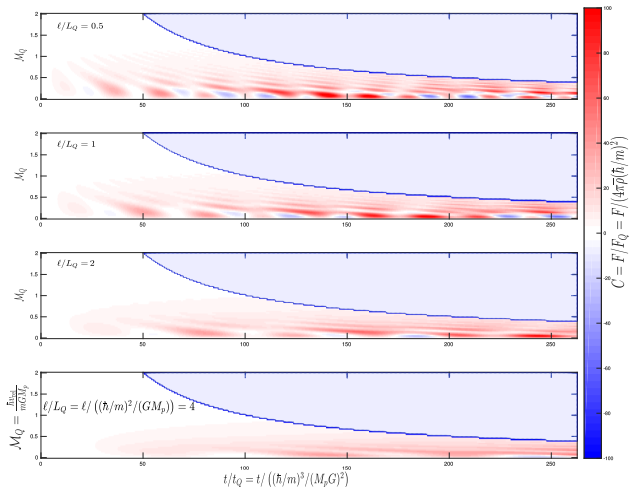


- ▶ constraint: $m_{\text{axion}} > 0.6 \times 10^{-22}$ eV

Dynamical Friction (PM, Lancaster in prep)

- ▶ Perturber of mass M_p , size ℓ . System is characterized by the quantum length scale $L_Q = (\hbar/m)^2/(GM_p)$

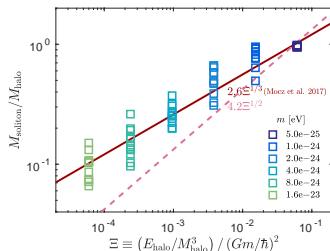
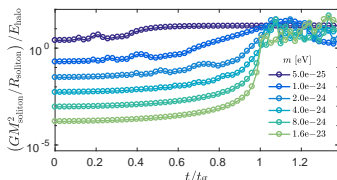
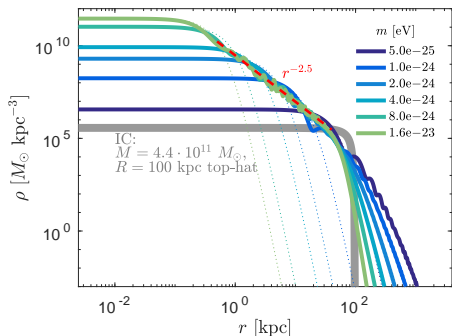
Dynamical Friction Coefficient



- ▶ **Dynamical friction coefficient C** encodes object size. Drag effective at low relative velocities, small perturber sizes

1D direct radial collapse (PM+ in prep)

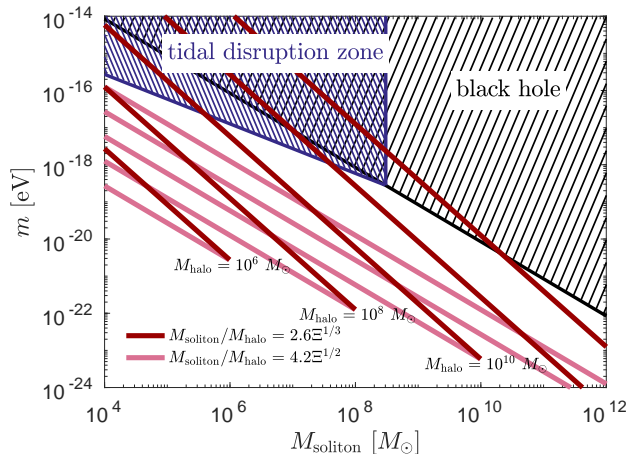
- ▶ What is the resulting soliton core mass after a free-fall time as a function of m_{boson} ?



- ▶ Soliton core energy is independent of m_{boson} , traces halo total energy

1D direct radial collapse (PM+ in prep)

- ▶ What is the fate of the soliton core?



Conclusions

- ▶ FDM is a physically-motivated alternative to CDM that modifies small-scale structure
- ▶ rich mathematical structure (SP-VP correspondence; Mocz et al. 2018)
- ▶ Small-scale features \Rightarrow astrophysical consequences
 - ▶ soliton cores (tidal disruptions? seed BHs?)
 - ▶ dynamical heating (random walk forcing field, disk thickening)
 - ▶ dynamical friction (from quantum pressure, effective at low relative velocities, small perturber sizes)

References I

- Armengaud E., Palanque-Delabrouille N., Yèche C., Marsh D. J. E., Baur J., 2017, *MNRAS*, 471, 4606 7
- Arvanitaki A., Dimopoulos S., Dubovsky S., Kaloper N., March-Russell J., 2010, *Phys. Rev. D*, 81, 123530 5
- Boylan-Kolchin M., Bullock J. S., Kaplinghat M., 2011, *MNRAS*, 415, L40 5
- , 2012, *MNRAS*, 422, 1203 5
- Chavanis P.-H., 2011, *Phys. Rev. D*, 84, 043531 3
- de Blok W. J. G., 2010, *Advances in Astronomy*, 2010, 789293 5
- Donato F. et al., 2009, *MNRAS*, 397, 1169 5
- Flores R. A., Primack J. R., 1994, *ApJ*, 427, L1 5
- Gentile G., Salucci P., Klein U., Vergani D., Kalberla P., 2004, *MNRAS*, 351, 903 5
- Gonzalez-Morales A. X., Marsh D. J. E., Peñarrubia J., Ureña-López L. A., 2016, *ArXiv e-prints* 8
- Hlozek R., Grin D., Marsh D. J. E., Ferreira P. G., 2015, *Phys. Rev. D*, 91, 103512 6
- Hlozek R., Marsh D. J. E., Grin D., 2017, *ArXiv e-prints* 6
- Hu W., Barkana R., Gruzinov A., 2000, *Physical Review Letters*, 85, 1158 3
- Iršič V., Viel M., Haehnelt M. G., Bolton J. S., Becker G. D., 2017, *Physical Review Letters*, 119, 031302 7
- Klypin A., Karachentsev I., Makarov D., Nasonova O., 2015, *MNRAS*, 454, 1798 5
- Klypin A., Kravtsov A. V., Valenzuela O., Prada F., 1999, *ApJ*, 522, 82 5
- Marsh D. J. E., Pop A.-R., 2015, *MNRAS*, 451, 2479 8
- Mocz P., Lancaster L., Fialkov A., Becerra F., Chavanis P.-H., 2018, *Phys. Rev. D*, 97, 083519 2, 23, (document), 38
- Mocz P., Succi S., 2015, *Phys. Rev. E*, 91, 053304 2, 14, (document), 17
- Mocz P., Vogelsberger M., Robles V. H., Zavala J., Boylan-Kolchin M., Fialkov A., Hernquist L., 2017, *MNRAS*, 471, 4559 2, 9, 14, (document)
- Moore B., 1994, *Nat*, 370, 629 5
- Moore B., Ghigna S., Governato F., Lake G., Quinn T., Stadel J., Tozzi P., 1999, *ApJ*, 524, L19 5
- Papastergis E., Martin A. M., Giovanelli R., Haynes M. P., 2011, *ApJ*, 739, 38 5
- Peebles P. J. E., 2000, *ApJ*, 534, L127 3
- Shive H.-Y., Liao M.-H., Woo T.-P., Wong S.-K., Chiueh T., Broadhurst T., Hwang W.-Y. P., 2014, *Physical Review Letters*, 113, 261302 3, 4, 12
- Schwabe B., Niemeyer J. C., Engels J. F., 2016, *Phys. Rev. D*, 94, 043513 3
- Zavala J., Jing Y. P., Faltenbacher A., Yepes G., Hoffman Y., Gottlöber S., Catinella B., 2009, *ApJ*, 700, 1779 5